

*Please show all work !!!

1. Change from degrees to radians: 240°

$$240 \times \frac{\pi}{180} = \frac{240\pi}{180} \div 30 = \frac{8\pi}{6} \div 2 = \boxed{\frac{4\pi}{3}}$$

2. Change from radians to degrees: $\frac{7\pi}{6}$

$$\frac{7\pi}{6} \cdot \frac{180}{\pi} = \boxed{210^\circ}$$

3. Find the length of an arc that subtends a central angle of 120° in a circle of radius 5 cm.

$$s = \theta \cdot r \rightarrow s = \frac{2\pi}{3} \cdot 5 = \boxed{\frac{10\pi}{3}}$$

change 120° to radians first

$$120^\circ \times \frac{\pi}{180} = \frac{120\pi}{180} \div 60 = \frac{2\pi}{3}$$

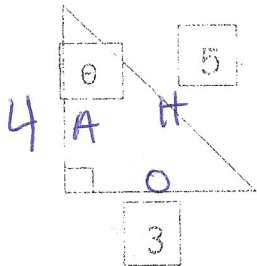
4. Find the area of a sector with central angle 90° in a circle with radius 6m.

$$A = \frac{1}{2} \theta \cdot r^2 \Rightarrow A = \frac{1}{2} \cdot \frac{\pi}{2} \cdot 6^2 = \frac{36\pi}{4} = \boxed{9\pi}$$

change 90° to radians

$$90^\circ \times \frac{\pi}{180} = \frac{90\pi}{180} \div 90 = \frac{\pi}{2}$$

5. Find the exact value of the six trig functions.



$\sin \theta = \frac{O}{H} = \frac{3}{5}$	$\csc \theta = \frac{H}{O} = \frac{5}{3}$
$\cos \theta = \frac{A}{H} = \frac{4}{5}$	$\sec \theta = \frac{H}{A} = \frac{5}{4}$
$\tan \theta = \frac{O}{A} = \frac{3}{4}$	$\cot \theta = \frac{A}{O} = \frac{4}{3}$

Use $a^2 + b^2 = c^2$

$$a^2 + 3^2 = 5^2$$

$$a^2 + 9 = 25 \quad \sqrt{a^2} = \sqrt{16}$$

$$\begin{matrix} -9 & -9 \end{matrix} \quad a = 4$$

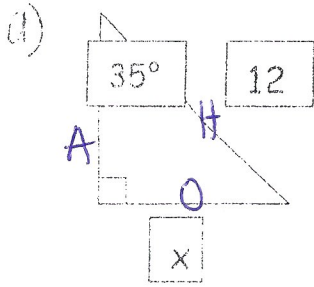
SOH
Esc

CAH
Sec

TOA
Cot

SOH CAH TOA

6. Find x.



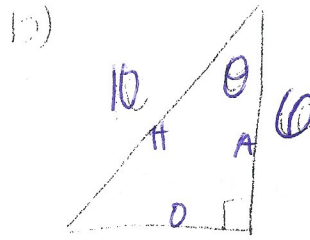
$$\sin \theta = \frac{O}{H}$$

~~$$\sin 35^\circ = \frac{x}{12}$$~~

$$x = 12 \cdot \sin 35^\circ$$

$$x = 6.88$$

Find θ



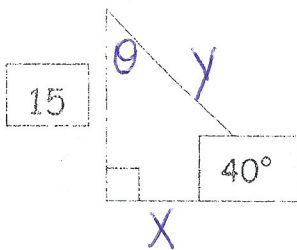
$$\cos \theta = \frac{A}{H}$$

$$\cos \theta = \frac{6}{10}$$

~~$$\cos \theta = 0.6$$~~

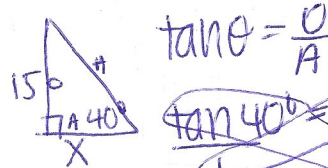
$$\theta = 53.1^\circ$$

7. Solve the right triangle.



$$\theta = 180 - (90 + 40)$$

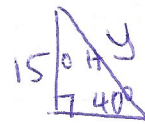
$$\theta = 50^\circ$$



$$\tan \theta = \frac{O}{A}$$

~~$$\tan 40^\circ = \frac{15}{x}$$~~

$$x \cdot \frac{\tan 40^\circ}{\tan 40^\circ} = \frac{15}{\tan 40^\circ} \quad x = 17.88$$



$$\sin \theta = \frac{O}{H}$$

~~$$\sin 40^\circ = \frac{15}{y}$$~~

$$y \cdot \frac{\sin 40^\circ}{\sin 40^\circ} = \frac{15}{\sin 40^\circ}$$

$$y = 23.34$$

**Find the exact value of the trig function.

$$8. \cot 210^\circ = \frac{x}{y} = \frac{-\frac{\sqrt{3}}{2}}{\frac{1}{2}} = +\frac{\sqrt{3}}{2} \cdot \frac{2}{1} = \sqrt{3}$$

$$9. \sin 300^\circ = y = \frac{-\sqrt{3}}{2}$$

$$10. \tan(-60^\circ) = \frac{y}{x} = \frac{-\sqrt{3}}{2} = -\frac{\sqrt{3}}{2}$$

$$11. \csc \frac{11\pi}{3} = \frac{1}{y} = \frac{1}{\frac{-\sqrt{3}}{2}} = -\frac{2}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$$

$$\frac{1}{-\frac{\sqrt{3}}{2}} = 1 \cdot \frac{-2}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$$