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Section # 1.1 Real Numbers

Standard=

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Properties of Real Numbers

- Commutative Property

$$a + b = b + a$$

$$ab = ba$$

- Associative Property

$$(a + b) + c = a + (b + c)$$

$$(ab)c = a(bc)$$

- Distributive Property

$$a(b + c) = ab + ac$$

$$(b + c)a = ab + ac$$

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Types of Real Numbers

- Natural Numbers: 1, 2, 3, 4, ...
- Integers: ..., -3, -2, -1, 0, 1, 2, 3, ...
- Rational Numbers: can be expressed as $\frac{m}{n}$ where $n \neq 0$

$$\text{Ex: } \frac{1}{3}, \frac{-2}{5}, .52 = \frac{52}{100}, 0.23 = \frac{23}{100}$$

- Irrational Numbers: A number that cannot be expressed as a ratio of integers

$$\text{Ex: } \sqrt{3}, \sqrt[3]{5}, \pi, \frac{5}{\pi}$$

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Example: State the property.

$$(a) \quad 2(a+b) = 2a+2b$$

$$(b) \quad 3(2x+1) = (2x+1)3$$

Example: Rewrite the expression using the given property.

(a) Associative Property of Multi.

$$7(3x) = (7 \cdot 3)x$$

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Example: List the elements of the given set that are natural numbers, integers, rational and irrational.

$$\{1.001, 0.333, \dots, -\pi, -11, 11, \frac{13}{15}, \sqrt{16}, 3.14, \frac{15}{3}\}$$

natural #s: 11, $\sqrt{16} = 4$, $\frac{15}{3} = 5$

integers: -11, 11, $\sqrt{16}$, $\frac{15}{3}$

rational #s: 1.001, 0.333, $\frac{13}{15}$, $\sqrt{16}$, 3.14, $\frac{15}{3}$, -11, 11,

irrational #s: $-\pi$

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Example: Write each statement in terms of inequalities.

(a) y is negative

$$y < 0$$

(b) x is greater than 1

$$x > 1$$

(c) x is at most 8

$$x \leq 8$$

(d) w is positive and is less than or equal to 17

$$0 < x \leq 17$$

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Sets and Intervals

Set = a collection of objects (numbers) called elements

Ex: Let S be a set

$a \in S$ means "a" is an element of S

$a \notin S$ means "a" is not an element of S

Writing Sets

- With Braces $S = \{1, 2, 3, 4, 5, 6\}$
- Set-builder notation $S = \{x \mid 0 < x < 7\}$

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Intervals

Open Intervals: from "a" to "b" consists of all numbers between "a" and "b" and is denoted by (a,b)

 $a < x < b$

Closed Interval: from "a" to "b" including the endpoints and is denoted by [a,b]

 $a \leq x \leq b$

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If S and T are sets, then the . . .

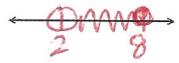
Union $S \cup T$ is the set of elements that are in S or T (or both)

Intersection $S \cap T$ is the set of elements that are in both S and T

Empty set ϕ is the set that contains no elements

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Example: Express the interval in terms of inequalities and then graph.

(a) (2,8]  $2 < x \leq 8$

(b) $(1, \infty)$ $x > 1$ 

Example: Express the inequality in interval notation and then graph.

(a) $x \geq -5$  $[-5, \infty)$

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Example: If $S = \{1, 3, 5, 6, 8\}$, $T = \{6, 8, 9, 10\}$ and $V = \{9, 10, 11\}$.

Find $S \cup T, S \cap T, S \cap V$.

everything in common

$S \cup T = \{1, 3, 5, 6, 8, 9, 10\}$

$S \cap T = \{6, 8\}$

$S \cap V = \phi$ empty set
no values in set

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Homework: 

Section #1.1: pg #10: 1-23 odd, 27-37 odd, 41-65 odd

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Section #1.2
Exponents and Radicals

STANDARD: ALGEBRA 2 REVIEW

④ Example: Evaluate.

(a) $5^2 \cdot \left(\frac{1}{5}\right)^3 = 5^2 \cdot \frac{1}{5^3} = \frac{1}{5}$

(b) $\frac{10^7}{10^4} = 10^3 = 1000$

(c) $\frac{3^5}{3^{-2}} = 3 \cdot 3^2 = 3^3 = 27$

(d) $\frac{2^4}{2^{-3}} = \frac{2^4 \cdot 2^3}{1} = \frac{2^7}{1} = 128$

(e) $\left(\frac{2}{3}\right)^{-3} = \left(\frac{3}{2}\right)^3 = \frac{3^3}{2^3} = \frac{27}{8}$

(f) $(3x^2)(4x^5) = 12x^7$

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<p>Zero Exponent</p> $a^0 = 1$	<p>Negative Exponent</p> $a^{-n} = \frac{1}{a^n}$
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EXAMPLE: EVALUATE

(A) $\left(\frac{4}{7}\right)^0 = 1$

(B) $x^{-1} = \frac{1}{x^1} = \frac{1}{x}$

(C) $(-2)^{-3} = \frac{1}{(-2)^3} = \frac{-1}{8}$

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(g) $\frac{x^5(2x)^3}{x^2} = \frac{x^5 \cdot 2^3 \cdot x^3}{x^2} = \frac{8x^8}{x^2} = 8x^6$

(h) $\frac{(2x^3)^2}{(x^3)} = \frac{2^2 x^6}{x^3} = \frac{4x^6}{x^3} = 4x^3$

(i) $(2x^3y^{-1}) \cdot \frac{1}{4}x^{-6} \cdot (4y^4) = 8x^{-3}y^3 = \frac{8y^3}{x^3}$

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Laws of Exponents

$a^m \cdot a^n = a^{m+n}$ $\frac{a^m}{a^n} = a^{m-n}$ $(a^m)^n = a^{mn}$ $(ab)^m = a^m b^m$	$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$ $\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n$ $\frac{a^{-n}}{b^{-m}} = \frac{b^m}{a^n}$
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Homework

SECTION=1.2
 PG=21: 9, 11, 27-43ODD

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Properties of Radicals

$$\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b} \qquad a^{\frac{1}{n}} = \sqrt[n]{a}$$

$$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}} \qquad a^{\frac{m}{n}} = (\sqrt[n]{a})^m = \sqrt[n]{a^m}$$

$$\sqrt[m]{\sqrt[n]{a}} = \sqrt[mn]{a}$$

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Example: Evaluate

(a) $25^{\frac{1}{2}} = \sqrt{25} = 5$

(b) $32^{\frac{2}{5}} = (\sqrt[5]{32})^2 = 2^2 = 4$

(c) $(\frac{27}{8})^{\frac{2}{3}} = (\sqrt[3]{\frac{27}{8}})^2 = (\frac{3}{2})^2 = \frac{9}{4}$

(d) $(2x^{\frac{3}{2}}(4x)^{\frac{1}{2}})^{\frac{2}{3}} = 2x^{\frac{3}{2} \cdot \frac{2}{3}} \cdot 4^{\frac{1}{2} \cdot \frac{2}{3}} x^{\frac{1}{2} \cdot \frac{2}{3}} = 2x^1 \cdot 4^{\frac{1}{3}} x^{\frac{1}{3}} = \frac{2x \cdot 4^{\frac{1}{3}} \cdot x^{\frac{1}{3}}}{4^{\frac{1}{3}}} = \frac{2x}{\sqrt[3]{4}} = \frac{2x}{2} = x$

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Example: Evaluate.

(a) $\sqrt{64} = 8$

(b) $\sqrt{72} = 6\sqrt{2}$

(c) $\sqrt{75} + \sqrt{48} = 5\sqrt{3} + 4\sqrt{3} = 9\sqrt{3}$

(d) $\sqrt[3]{64} = \sqrt[3]{4^3} = 4$

(e) $\sqrt[5]{-32} = \sqrt[5]{(-2)^5} = -2$

(f) $\sqrt[3]{\frac{8}{125}} = \sqrt[3]{\frac{2^3}{5^3}} = \frac{2}{5}$

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(e) $(8x^6)^{\frac{2}{3}} = (\sqrt[3]{8x^6})^2 = (\sqrt[3]{8} \cdot \sqrt[3]{x^6})^2 = (2x^2)^2 = 4x^4$

(f) $(4x^6y^8)^{\frac{3}{2}} = (\sqrt{4x^6y^8})^3 = (2x^3y^4)^3 = 8x^9y^{12}$

(g) $\frac{1}{\sqrt{5}} \sqrt{5} = \frac{\sqrt{5}}{\sqrt{5}} = 1$

(h) $\sqrt{\frac{x}{6}} \sqrt{\frac{6}{x}} = \sqrt{\frac{6x}{6x}} = \sqrt{1} = 1$

3 | 75
5 | 25
5

3 | 48
4 | 12
4

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(g) $\sqrt[5]{g^{10}} = \sqrt[5]{(g^2)^5} = g^2$

(h) $\sqrt[3]{x^3y^6} = xy^2$

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Homework

SECTION=1.2
PG=21
1-ODD, 13-1-ODD, 23, 25, 45-4-ODD,
53-61-ODD, 83, 85

Section#1.3
Algebraic Expressions

Standard: Algebra 2 Review

Example: Factor out the common factor.

(a) $\frac{2x^2(2x^4 + 4x^3 - 14x^2)}{x^2 + 2x - 7} = 2x^2(x^2 + 2x - 7)$

(b) $\frac{(z+2)^2 - 5(z+2)}{(z+2) - 5} = \frac{(z+2)(z+2-5)}{z-3} = (z+2)(z-3)$

Types of Polynomials

Monomial-one term
Binomial-two terms
Trinomial-three terms

Example: State the type of polynomial, then list the terms and state its degree.

(a) $2x^5 + 4x^2$ Binomial, degree = 5
Terms: $2x^5, 4x^2$

(b) $x - x^2 + \sqrt{3}x^3$ Trinomial, degree = 3
Terms: $x, -x^2, \sqrt{3}x^3$

Example: Factor.

(a) $x^2 + 7x + 12 = (x+3)(x+4)$

(b) $x^2 + 3x - 18 = (x+6)(x-3)$

(c) $x^2 + 3x - 10 = (x+5)(x-2)$

(d) $6x^2 + x - 12 = (2x+3)(3x-4)$

(e) $4x^2 - 13x - 12 = (x-4)(4x+3)$

Example: Perform the indicated operation and simplify.

(a) $(5 - 3x) + (2x - 8) = -x - 3$

(b) $(3x^2 + x + 1) - (2x^2 - 3x - 5) = x^2 + 4x + 6$

(c) $4(x^2 - 3x + 5) - 3(x^2 - 2x + 1) = 4x^2 - 12x + 20 - 3x^2 + 6x - 3 = x^2 - 6x + 17$

(d) $(4x - 3)(2x + 5y) = 8x^2 + 20xy - 6xy - 15y^2 = 8x^2 + 14xy - 15y^2$

Homework

Section=1.3
Pg=31: 3-5+ multiples of 3's

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Special Factoring Formulas

$A^2 - B^2 = (A - B)(A + B)$
 $(A + B)^2 = A^2 + 2AB + B^2$
 $(A - B)^2 = A^2 - 2AB + B^2$
 $A^3 + B^3 = (A + B)(A^2 - AB + B^2)$
 $A^3 - B^3 = (A - B)(A^2 + AB + B^2)$

Example: Factor completely.

(a) $12x^3 + 18x$
 $2x^2 - 3$
 $6x(2x^2 - 3)$

(c) $3x^3 - 27x$
 $3x(x^2 - 9)$
 $3x(x+3)(x-3)$

(b) $9x^2 - 36x - 45$
 $9(x^2 - 4x - 5)$
 $9(x-5)(x+1)$

(d) $x^6 - 8y^3$
 $(x^2 - 2y)(x^4 + 2x^2y + 4y^2)$

Example: Factor.

(a) $4x^2 - 25$
 $(2x - 5)(2x + 5)$

(b) $49y^2 - 1$
 $(7y - 1)(7y + 1)$

(c) $x^2 + 12x + 36$
 $(x + 6)^2$

(d) $25x^2 - 10xy + y^2$
 $(5x - y)^2$

(e) $27x^3 - 1$
 $(3x - 1)(9x^2 + 3x + 1)$

(f) $x^6 + 8$
 $(x^2 + 2)(x^4 - 2x^2 + 4)$

Homework

Section=1.3
Pg=31: 57-96 multiples of 3's



Example: Factor by grouping.

(a) $x^3 + x^2 + 4x + 4$
 $\frac{x^3 + x^2}{x+1} + \frac{4x + 4}{x+1}$
 $(x+1)(x^2 + 4)$

(b) $x^3 - 2x^2 - 3x + 6$
 $\frac{x^3 - 2x^2}{x-2} - \frac{3x + 6}{x-2}$
 $(x-2)(x^2 - 3)$

Pre-calculus

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Section #1.4

Rational Expressions

Standard # Algebra 2 Review

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Example: Multiply or divide. Then simplify.

(a) $\frac{x^2-25}{x^2-16} \cdot \frac{x+4}{x+5}$ (b) $\frac{x^2-x-6}{x^2+2x} \cdot \frac{x^3+x^2}{x^2-2x-3}$

$$\frac{(x+5)(x-5)(x+4)}{(x+4)(x-4)(x+5)} = \frac{x-5}{x-4}$$

$$\frac{(x-3)(x+2) \cdot x^2(x+1)}{x(x+2)(x-3)(x+1)} = \frac{x(x+1)}{(x+1)} = x$$

$$\begin{array}{r} y \quad 2y \quad -3y \quad 2y \\ 6 \quad 12 \quad 9 \quad 3 \end{array}$$

$$\begin{array}{r} 2y \quad -6 \quad 2y \quad y \\ 3 \quad 1 \quad 1 \quad -1 \end{array}$$

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The domain of an algebraic expression is the set of numbers that the variable can represent.

Example: Find the domain.

(a) $-x^4 + x^3 + 9x$
all real #s

(b) $\frac{2x^2-5}{3x+6}$
 $3x+6 \neq 0$
 $3x \neq -6$
 $x \neq -2$
 all real #s except $x = -2$

(c) $\frac{1}{\sqrt{x-1}} \geq 0$
 $x-1 \geq 0$
 $x \geq 1$

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(c) $\frac{4y^2-9}{2y^2+9y-18} \div \frac{2y^2+y-3}{y^2+5y-6}$

$$\frac{(2y-3)(2y+3)}{(2y-3)(y+6)} \div \frac{(2y+3)(y-1)}{(y+6)(y-1)}$$

$$\frac{(2y-3)(2y+3)}{(2y-3)(y+6)} \cdot \frac{(y+6)(y-1)}{(2y+3)(y-1)} = 1$$

$$\begin{array}{r} 2y \quad 6 \quad 2y \\ 3 \quad 5 \end{array}$$

$$\begin{array}{r} 7y \quad 10 \quad 3 \\ 1 \quad 3 \end{array}$$

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Example: Simplify

(a) $\frac{x^2-x-2}{x^2-1}$

$$\frac{(x-2)(x+1)}{(x+1)(x-1)} = \frac{x-2}{x-1}$$

(b) $\frac{y^2-3y-18}{2y^2+5y+3}$

$$\frac{(y-6)(y+3)}{(2y+3)(y+1)}$$

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Example: Add or subtract. Then simplify.

(a) $\frac{2x-1}{x+4} - \frac{1}{x+4}$ (b) $\frac{x^2+6x}{x-4} - \frac{3}{x+6}$

$$\frac{2x-1-(x+4)}{x+4} = \frac{2x-1-x-4}{x+4} = \frac{x-5}{x+4}$$

$$\frac{x^2+6x-(3x-12)}{(x-4)(x+6)} = \frac{x^2+6x-3x+12}{(x-4)(x+6)} = \frac{x^2+3x+12}{(x-4)(x+6)}$$

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(c) $\frac{x}{x^2-4} + \frac{1}{x-2}$ (d) $\frac{x}{x^2-x-6} - \frac{1}{x+2} - \frac{2}{x-3}$

$\frac{x}{(x+2)(x-2)} + \frac{1}{(x-2)(x+2)}$ $\frac{x}{(x-3)(x+2)} - \frac{1}{(x+2)} - \frac{2}{(x-3)}$

$\frac{x+x+2}{(x+2)(x-2)}$ $\frac{x-x+3-2x-4}{(x-3)(x+2)}$

$\frac{2x+2}{(x+2)(x-2)}$ $\frac{-2x-1}{(x-3)(x+2)}$

$\frac{2(x+1)}{(x+2)(x-2)}$ $\frac{-2x-1}{(x-3)(x+2)}$

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Example: Rationalize.

(a) $\frac{2}{3-\sqrt{5}} \cdot \frac{(3+\sqrt{5})}{(3+\sqrt{5})} = \frac{6+2\sqrt{5}}{9-5}$

$\frac{6+2\sqrt{5}}{4} \div 2$

$\frac{3+\sqrt{5}}{2}$

⑨

Homework

»» Section#1.4: pg#41
1-25odd, 31-47odd,
51, 73, 75

Pre-calculus

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Section #1.5
Equations

Standard# Algebra 2 Review

④

Example: Solve for the indicated variable.

(a) $P = 2l + 2w$, solve for w .

$$P = 2l + 2w$$

$$-2l - 2l$$

$$\frac{P - 2l}{2} = \frac{2w}{2}$$

$$w = \frac{P - 2l}{2}$$

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Example: Determine whether the given values are a solution.

(a) $1 - [2 - (3 - x)] = 4x - (6 + x)$

$$1 - [2 - 3 + x] = 4x - 6 - x$$

$$1 - 2 + 3 - x = 3x - 6$$

$$-x + 2 = 3x - 6$$

$$+x + 6 \quad +x + 6$$

$$8 = 4x \quad \boxed{x = 2}$$

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Example: Solve by factoring.

(a) $x^2 + 3x - 4 = 0$ (b) $2y^2 + 7y + 3 = 0$

$$(x+4)(x-1) = 0$$

$$x+4=0 \quad x-1=0$$

$$\boxed{x = -4 \quad x = 1}$$

$$\begin{array}{r} 2y^2 + 7y + 3 = 0 \\ \hline 2y \quad 1 \\ 3 \quad 3 \end{array}$$

$$(2y+1)(y+3) = 0$$

$$2y+1=0 \quad y+3=0$$

$$\boxed{y = -\frac{1}{2} \quad y = -3}$$

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Example: Solve.

$$(a) \frac{x}{5} = \frac{3}{10}x + 7$$

$$2x = 3x + 70$$

$$-3x - 3x$$

$$-x = 70$$

$$\boxed{x = -70}$$

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Example: Solve by completing the square.

(a) $x^2 - 4x + 2 = 0$ (b) $x^2 + 3x - \frac{7}{4} = 0$

$$x^2 - 4x + 4 = -2 + 4 \quad x^2 + 3x + \frac{9}{4} = \frac{7}{4} + \frac{9}{4}$$

$$\frac{-4}{2} \rightarrow (-2)^2 \quad \frac{3}{2} \rightarrow \left(\frac{3}{2}\right)^2$$

$$\sqrt{(x-2)^2} = \sqrt{2}$$

$$x-2 = \pm\sqrt{2}$$

$$\boxed{x = 2 \pm \sqrt{2}}$$

$$\sqrt{\left(x + \frac{3}{2}\right)^2} = \sqrt{4}$$

$$x + \frac{3}{2} = \pm 2$$

$$x = -\frac{3}{2} \pm 2$$

$$\boxed{x = \frac{1}{2}, -\frac{7}{2}}$$

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Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

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Homework

Section #1.5: pg#55

1, 5-15odd, 23, 25, 37-41odd, 45-47odd, 53-57odd, 69, 81, 96

⑧

Example: Solve using the quadratic formula.

(a) $3x^2 + 7x + 4 = 0$

$a=3 \quad b=7 \quad c=4$

$$x = \frac{-7 \pm \sqrt{49 - 4(3)(4)}}{2(3)} = \frac{-7 \pm \sqrt{1}}{6}$$

$$= \frac{-7 \pm 1}{6}$$

$$= \frac{-7+1}{6} = \frac{-6}{6} = -1$$

$$= \frac{-7-1}{6} = \frac{-8}{6} = -\frac{4}{3}$$

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Example: Find all real number solutions.

(a) $\sqrt{5-x} + 1 = x - 2$ (b) $|2x+1| = 3$

$$\sqrt{5-x} = (x-3)^2 \quad 2x+1=3 \quad 2x+1=3$$

$$5-x = x^2 - 6x + 9 \quad 2x=2 \quad 2x=-4$$

$$x^2 - 5x + 4 = 0 \quad \boxed{x=1} \quad \boxed{x=-2}$$

$x^2 - 5x + 4 = 0$

$(x+4)(x-1) = 0$

$$\boxed{x=4} \quad \boxed{x=-1}$$

Pre-cal

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Standard# Algebra 2 Review
**SECTION#1.7
INEQUALITIES**

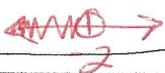
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Guidelines for Solving Nonlinear Inequalities

1. Move all terms to one side
2. Factor
3. Find intervals
-Determine the values for which each factor is zero
4. Make a table
-Use test values to make a table of the signs(+/-) of each factor
5. Solve

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Example: Solve. Express the solution using interval notation and graph.

(a) $3x+11 < 5$
 $-11 -11$
 $3x < -6$
 $x < -2$
 $(-\infty, -2)$


(b) $6-x \geq 2x+9$
 $+x +x$
 $6 \geq 3x+9$
 $-9 -9$
 $-3 \geq 3x$
 $-1 \geq x$
 $x \leq -1$
 $(-\infty, -1]$


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Example: Solve.

(a) $\frac{2x+6}{x-2} \leq 0$ *less than < (neg)*

$2x+6=0$ $x-2=0$
 $2x=-6$ $x=2$
 $x=-3$

-3 $+$ $-$ $+$


③

(c) $5 \leq 3x-4 \leq 14$ (d) $1 < 3x+4 \leq 16$

$+4 +4 +4$ $-4 -4 -4$

$9 \leq 3x \leq 14$ $-3 < 3x \leq 12$
 $\frac{9}{3} \leq \frac{3x}{3} \leq \frac{14}{3}$ $\frac{-3}{3} < \frac{3x}{3} \leq \frac{12}{3}$

$3 \leq x \leq \frac{14}{3}$ $-1 < x \leq 4$
 $[3, \frac{14}{3}]$ $(-1, 4]$



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(b) $(x-5)(x+4) \geq 0$ (c) $x^2+5x+6 > 0$

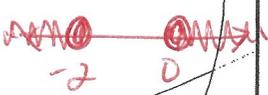
$x-5=0$ $x+4=0$ $(x+3)(x+2) > 0$
 $x=5$ $x=-4$ $x+3=0$ $x+2=0$
 $x=-3$ $x=-2$

$+$ $-$ $+$ $-$


$(-\infty, -4] \cup [5, \infty)$ $(-\infty, -3) \cup (-2, \infty)$

$\frac{6}{3} \times \frac{2}{5}$

⑦

(d) $ 3x < 15$		(e) $ x+1 \geq 1$	
$\frac{3x}{3} < \frac{15}{3}$	$\frac{3x}{3} > \frac{-15}{3}$	$x+1 \geq 1$	$x+1 \leq -1$
$x < 5$	$x > -5$	$x \geq 0$	$x \leq -2$
			
$(-5, 5)$		$(-\infty, -2] \cup [0, \infty)$	

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Section#1.7
Pg#84: 7-13odd, 21-25odd, 29-35odd, 47, 51, 63-67odd

HOMEWORK

Pre-calculus

Section#1.10
Lines

Standard# Algebra 2 Review

Important Formulas

Slope-intercept form	$y = mx + b$
Point-slope form	$y - y_1 = m(x - x_1)$
General Form	$Ax + By + C = 0$
Vertical line through (a,b)	$x = a$
Horizontal line through (a,b)	$y = b$

Slope of a line

$$m = \frac{\text{rise}}{\text{run}} = \frac{y_1 - y_2}{x_1 - x_2}$$

Stack and Subtract

Example: Find an equation of the line that satisfies the given conditions.

(a) Through $(-2, 4)$; slope -1 .

(b) Through $(-1, -2)$ and $(4, 3)$.

Handwritten work for (a):

$$y = mx + b$$

$$4 = (-1)(-2) + b$$

$$4 = 2 + b$$

$$-2 = -2$$

$$2 = b$$

$$y = -x + 2$$

Handwritten work for (b):

$$\frac{3 - (-2)}{4 - (-1)} = \frac{5}{5} = 1 = m$$

$$y = mx + b$$

$$3 = 1(4) + b$$

$$3 = 4 + b$$

$$-1 = b$$

Final equations:

$$y = x - 1$$

$$x - y - 1 = 0$$

Example: Find the slope.

(a) $(1, 2)$ and $(3, 3)$

$$\frac{3 - 2}{3 - 1} = \frac{1}{2}$$

(b) $(2, -5)$ and $(-4, 3)$

$$\frac{3 - (-5)}{-4 - 2} = \frac{8}{-6} = -\frac{4}{3}$$

(c) x-intercept -8 ; y-intercept 6 .

(d) Through $(3, 2)$ and parallel to $4x + 6y + 5 = 0$.

Handwritten work for (c):

$$(-8, 0) \quad (0, 6)$$

$$b = 6$$

$$y = mx + b$$

$$0 = m(-8) + 6$$

$$-6 = -8m$$

$$\frac{6}{8} = m$$

$$\frac{3}{4} = m$$

$$y = \frac{3}{4}x + 6$$

Handwritten work for (d):

$$y = mx + b$$

$$2 = -\frac{2}{3}(5) + b$$

$$\frac{2}{3} = -\frac{10}{3} + b$$

$$+\frac{10}{3} + \frac{10}{3}$$

$$\frac{16}{3} = b$$

$$y = -\frac{2}{3}x + \frac{16}{3}$$

$$3y = -2x + 16$$

$$2x + 3y - 16 = 0$$

Handwritten equations:

$$y = \frac{3}{4}x + 6$$

$$4y = 3x + 24$$

$$3x - 4y + 24 = 0$$

$$y = -\frac{2}{3}x + \frac{16}{3}$$

$$3y = -2x + 16$$

$$2x + 3y - 16 = 0$$

(e) Through $(-1, -2)$ and perpendicular to $2x+5y+8=0$.

$$\frac{dy}{dx} = \frac{-2x-8}{5} \quad y = mx+b$$

$$y = \frac{-2}{5}x - \frac{8}{5} \quad -2 = \frac{5}{2}(-1) + b$$

$$\boxed{m = \frac{5}{2}} \quad -\frac{4}{2} - 2 = \frac{-5}{2} + b$$

$$\frac{+5}{2} \quad \frac{+5}{2}$$

$$\frac{1}{2} = b$$

$$y = \frac{5}{2}x + \frac{1}{2}$$

$$2y = 5x + 1$$

$$\boxed{5x - 2y + 1 = 0}$$

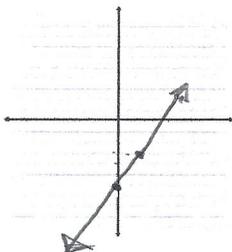
Example: Find the slope and y-intercept.
Then graph.

(a) $3x - 2y = 12$

$$\frac{-2y}{-2} = \frac{-3x+12}{-2}$$

$$y = \frac{3}{2}x - 6$$

$$m = \frac{3}{2} \quad b = -6$$



Homework

Section#1.10

Pg#120: 1-7odd, 11-31odd, 41-45odd