

Name: Answer key (11)

Date: \_\_\_\_\_

Period: \_\_\_\_\_

Pre-calculus

11.1-11.3

Review

Find the first four terms and the 100<sup>th</sup> term.

plug in 1, 2, 3, 4 and 100 for n!

1.  $a_n = \frac{(-1)^n}{n^2}$

$a_1 = \frac{(-1)^1}{1^2} = -\frac{1}{1} = \boxed{-1}$

$a_2 = \frac{(-1)^2}{2^2} = \boxed{\frac{1}{4}}$

$a_3 = \frac{(-1)^3}{3^2} = \boxed{-\frac{1}{9}}$

$a_4 = \frac{(-1)^4}{4^2} = \boxed{\frac{1}{16}}$

$a_{100} = \frac{(-1)^{100}}{100^2} = \boxed{\frac{1}{10000}}$

2.  $a_n = n^2 + 1$

$a_1 = 1^2 + 1 = 1 + 1 = \boxed{2}$

$a_2 = 2^2 + 1 = 4 + 1 = \boxed{5}$

$a_3 = 3^2 + 1 = 9 + 1 = \boxed{10}$

$a_4 = 4^2 + 1 = 16 + 1 = \boxed{17}$

$a_{100} = 100^2 + 1 = 10000 + 1 = \boxed{10001}$

Find the sum.

3.  $\sum_{k=1}^3 \frac{1}{k}$

plug in 1, 2, 3 for k, then add up

$\frac{1}{1} + \frac{1}{2} + \frac{1}{3} =$   
common denominator

$\frac{6}{6} + \frac{3}{6} + \frac{2}{6} = \frac{11}{6} = \boxed{\frac{15}{6}}$

4.  $\sum_{k=1}^4 k^2$

plug in 1, 2, 3, 4 for k, then add up

$1^2 + 2^2 + 3^2 + 4^2$

$1 + 4 + 9 + 16 = \boxed{30}$

Rewrite each series using sigma notation.

5.  $2 + 4 + 6 + 8 + 10$

$2(1) + 2(2) + 2(3) + 2(4) + 2(5)$

$$\boxed{\sum_{k=1}^5 2k}$$

Find the nth term of the arithmetic sequence. **use formula  $a_n = a + (n-1)d$**   
**plug in a, d & n**

6.  $a = 3, d = 5$

$$a_n = 3 + (n-1) \cdot 5$$

7.  $a = -6, d = 3$

$$a_n = -6 + (n-1) \cdot 3$$

Find the partial sum  $S_n$  of the arithmetic sequence that satisfies the given conditions.

**use formula  $S_n = \frac{n}{2} [2a + (n-1)d]$**

**plug in a, d & n**

8.  $a = 1, d = 2, n = 10$

$$\begin{aligned} S_{10} &= \frac{10}{2} [2 \cdot 1 + (10-1) \cdot 2] \\ &= 5 [2 + (9) \cdot 2] \\ &= 5 [2 + 18] = 5 \cdot 20 = \boxed{100} \end{aligned}$$

9.  $a = 3, d = 2, n = 12$

$$\begin{aligned} S_{12} &= \frac{12}{2} [2 \cdot 3 + (12-1) \cdot 2] \\ &= 6 [6 + (11) \cdot 2] \\ &= 6 [6 + 22] = 6 \cdot 28 = \boxed{168} \end{aligned}$$

A partial sum of an arithmetic sequence is given. Find the sum.

10.  $1 + 5 + 9 + \dots + 401$   $d = 4$

**use  $S_n = n \left( \frac{a + a_n}{2} \right)$  to find the sum**

**first use  $a_n = a + (n-1)d$  to find n.**

$a = 1, a_n = 401, n = 101$

*Solve for n*

$$\begin{aligned} a_n &= a + (n-1)d \\ 401 &= 1 + (n-1)4 \\ 401 &= 1 + 4n - 4 \end{aligned}$$

$$\begin{aligned} 401 &= 4n - 3 \\ +3 & \quad +3 \\ 404 &= 4n \\ \frac{404}{4} &= \frac{4n}{4} \\ 101 &= n \end{aligned}$$

$$\begin{aligned} S_{101} &= 101 \left( \frac{1 + 401}{2} \right) \\ &= 101 \left( \frac{402}{2} \right) = 101 (201) \\ &= \boxed{20,301} \end{aligned}$$

Find the nth term of the geometric sequence. Then find the fourth term.

**use formula  $a_n = ar^{n-1}$**

11.  $a = 3, r = 5$

$$a_n = 3 \cdot 5^{n-1}$$

$$\begin{aligned} a_4 &= 3 \cdot 5^{4-1} \\ &= 3 \cdot 5^3 \\ &= 3 \cdot 125 \\ &= \boxed{375} \end{aligned}$$

Find the first five terms and find the ratio  $r$ . **plug in 1, 2, 3, 4, 5 for  $n$**

12.  $a_n = 3^{n-1}$

$$a_1 = 3^{1-1} = 3^0 = \boxed{1}$$

$$a_2 = 3^{2-1} = 3^1 = \boxed{3}$$

$$a_3 = 3^{3-1} = 3^2 = \boxed{9}$$

$$a_4 = 3^{4-1} = 3^3 = \boxed{27}$$

$$a_5 = 3^{5-1} = 3^4 = \boxed{81}$$

1, 3, 9, 27, 81  
 $\underbrace{\quad}_{\times 3}$   $\underbrace{\quad}_{\times 3}$   $\underbrace{\quad}_{\times 3}$  times 3 each time

$r = \boxed{3}$

Find the partial sum  $S_n$  of the geometric sequence.

**Use formula  $S_n = a \cdot \frac{1-r^n}{1-r}$**

13.  $a = 5, r = 2, n = 6$

$$S_6 = 5 \cdot \frac{1-2^6}{1-2} = 5 \cdot \frac{1-64}{-1} = 5 \cdot \frac{-63}{-1} = 5 \cdot 63 = \boxed{315}$$

Find the sum of the geometric series. **Use  $S_n = a \cdot \frac{1-r^n}{1-r}$  to find the sum** where  $a = 1$

14.  $1 + 3 + 9 + \dots + 2187$   
 $\underbrace{\quad}_{\times 3}$   $\underbrace{\quad}_{\times 3}$   $r = 3$

**Use  $a_n = a \cdot r^{n-1}$  first to find  $n$**

$a = 1$   
 $a_n = 2187$   
 $r = 3$

$$2187 = 1 \cdot 3^{n-1}$$

plug in to see what makes  $n$  true  
 $3^8 - 1 = 3^7 = 2187$   
 $n = 8$

$$S_8 = 1 \cdot \frac{1-3^8}{1-3}$$

$$= \frac{1-6561}{-2}$$

$$= \frac{-6560}{-2}$$

$$= \boxed{3280}$$

Find the sum of the infinite geometric series.

15.  $1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \dots$   
 $\underbrace{\quad}_{\times \frac{1}{3}}$   $\underbrace{\quad}_{\times \frac{1}{3}}$   $r = \frac{1}{3}$

$a = 1$   
 $r = \frac{1}{3}$

$$S = \frac{1}{1 - \frac{1}{3}} = \frac{1}{\frac{3}{3} - \frac{1}{3}} = \frac{1}{\frac{2}{3}}$$

flip

$$= 1 \cdot \frac{3}{2} = \boxed{\frac{3}{2}}$$

16.  $1 - \frac{1}{2} + \frac{1}{4} - \frac{1}{8} + \dots$   
 $\underbrace{\quad}_{\times -\frac{1}{2}}$   $\underbrace{\quad}_{\times -\frac{1}{2}}$   $r = -\frac{1}{2}$

$a = 1$   
 $r = -\frac{1}{2}$

$$S = \frac{1}{1 + \frac{1}{2}}$$

$$S = \frac{1}{\frac{2}{2} + \frac{1}{2}} = \frac{1}{\frac{3}{2}}$$

flip

$$= 1 \cdot \frac{2}{3} = \boxed{\frac{2}{3}}$$