

AP Calculus Practice Exam
 AB Version – Section 1 – Part A

Calculators are NOT permitted on this portion of the exam. 28 questions = 55 minutes

plug in composition

1. Give $f(g(-2))$, given that $f(x) = x - 2$, $g(x) = \frac{x}{x^2 + 1}$

- a. $\frac{-11}{5}$ b. $\frac{-4}{17}$ c. -3 d. $\frac{14}{85}$ e. $\frac{-12}{5}$

$g(-2) = \frac{-2}{(-2)^2 + 1} = \frac{-2}{4 + 1} = \frac{-2}{5}$

$f\left(\frac{-2}{5}\right) = \frac{-2}{5} - \frac{2 \cdot 5}{1 \cdot 5} = \frac{-2}{5} - \frac{10}{5} = \frac{-12}{5}$

derivative

2. Find the slope of the tangent line to the graph of f at $x = 4$, given that $f(x) = x^2 - 6\sqrt{x}$

- a. $\frac{11}{2}$ b. $\frac{17}{2}$ c. $\frac{19}{2}$ d. $\frac{13}{2}$ e. $\frac{9}{2}$

$x^2 - 6x^{1/2}$

$2x - 6 \cdot \frac{1}{2}x^{-1/2}$

leading terms

3. Determine $\lim_{x \rightarrow \infty} \frac{3x^3 + x}{4x^5 + 3x^2 - 2}$

- a. 1 b. $\frac{3}{4}$ c. $\frac{9}{20}$ d. 0 e. ∞

$\frac{3x^3}{4x^5} = \frac{3}{4x^2} \rightarrow 0$ at $x=4$

$2x - \frac{3}{\sqrt{x}} = 2 \cdot 4 - \frac{3}{\sqrt{4}} = 8 - \frac{3}{2} = \frac{16}{2} - \frac{3}{2} = \frac{13}{2}$

4. $f(x) = x^3$. A region is bounded between the graphs of $y = -1$ and $y = f(x)$ for x between -1 and 0 , and between the graphs of $y = 1$ and $y = f(x)$ for x between 0 and 1 . Give an integral that corresponds to the area of this region.

- a. $\int_{-1}^1 1 + x^3 dx$ b. $\int_{-1}^1 1 - x^3 dx$ c. $\int_0^1 2(1 + x^3) dx$
 d. $\int_0^1 -x^3 - 1 dx$ e. $\int_0^1 2(1 - x^3) dx$

derivative find dy/dx

5. Given that $5x^3 - 3xy - 2y^2 = 1$, determine the change in y with respect to x .

- a. $-\frac{15x^2 - 3}{-3x - 4y}$ b. $-\frac{15x^2 - 3y}{-3 - 4y}$ c. $-\frac{15x^2 - 3y}{-3x - 4y}$ d. $-\frac{15x^2 - 3}{-3 - 4y}$ e. $-\frac{10x - 3y}{-3x - 2}$

$\frac{d(5x^3)}{dx} \cdot \frac{d(3xy)}{dx} - \frac{d(2y^2)}{dx} = d(1)$

$15x^2 - 3 \left[x \frac{dy}{dx} + y \frac{dx}{dx} \right] - 4y \frac{dy}{dx} = 0$
 $15x^2 - 3x \frac{dy}{dx} + 3y - 4y \frac{dy}{dx} = 0$

$-3 \frac{d}{dx} (x^2) + 5 \frac{d}{dx} (\csc x)$

$\frac{(-3x + 4y) dy}{-3x + 4y} = \frac{15x^2 - 3y}{-3x + 4y}$

derivative

6. Compute the derivative of $-3\sec x + 5\csc x$

- a. $-3\tan^2 x - 5\cot^2 x$ b. $-3\sec^2 x - 5\csc^2 x$ c. $-3\sec x \tan x + 5\csc x \cot x$
 d. $-3\sec x \tan x - 5\csc x \cot x$ e. $-3\csc x - 5\sec x$

$-3 \cdot \sec x \tan x + 5 \cdot (-\csc x \cot x)$
 $-3\sec x \tan x - 5\csc x \cot x$

7. Compute $\int_0^{\frac{1}{4}} \frac{16}{1 + 16t^2} dt$

- a. 4π b. 3π c. 0 d. $-\pi$ e. π

$$\frac{2x^4 + 4x \frac{d}{dx}(2x^4 - 4x) - 2x^4 - 4x \frac{d}{dx}(2x^4 + 4x)}{(2x^4 + 4x)^2}$$

derivative
quotient rule

8. Determine $\frac{d}{dx} \frac{2x^4 - 4x}{2x^4 + 4x}$

a. $\frac{48x^2 - 1}{(2x^3 + 4)^2}$

b. $\frac{12x^2}{(x^3 + 2)^2}$

c. $\frac{24x^2 - 1}{(2x^3 + 4)^2}$

d. $\frac{24x^2}{(2x^3 + 4)^2}$

e. $\frac{12x^2}{(2x^3 + 4)^2}$

$$\frac{(2x^4 + 4x)(8x^3 - 4) - (2x^4 - 4x)(8x^3 + 4)}{(2x^4 + 4x)^2}$$

$$16x^7 - 8x^4 + 32x^4 - 16x^7 - 1(16x^7 + 8x^4 - 32x^7 - 16x^4)$$

derivative
of find slope

9. Give the equation of the normal line to the graph of $y = 4x\sqrt{x^2 + 4} - 2$ at the point $(0, -2)$.

a. $8x + y = -2$

b. $x - 8y = 16$

c. $x + 8y = -16$

d. $-8x + y = -2$

e. $x + 8y = -2$

perpendicular line

$$\frac{-1(6x^4 + 64x^4)}{(2x^4 + 4x)^2}$$

$$\frac{4x^8 + 16x^5 + 16x^2}{(2x^4 + 4x)^2}$$

$$\frac{12x^2}{(x^3 + 2)^2}$$

f11
y=0 concave up
y<0 concave down

10. Determine the concavity of the graph of $f(x) = 4\sin x + 4\cos^2 x$ at $x = \pi$

a. -8

b. -6

c. -11

d. 4

e. 8

11. Compute $\int 4x^2 \sqrt{x^3 + 3} dx$.

a. $\frac{16}{9}(x^3 + 3)^{3/2} + c$

b. $\frac{8}{9}(x^3 + 3)^{3/2} + c$

c. $\frac{8}{3}(x^3 + 3)^{3/2} + c$

d. $\frac{4}{3\sqrt{x^3 + 3}} + c$

e. $\frac{8}{3\sqrt{x^3 + 3}} + c$

derivative
= 0

12. Give the value of x where the function $f(x) = x^3 + \frac{15}{2}x^2 + 12x - 2$ has a local minimum.

a. 1

b. -1

c. -4

d. 4

e. -3

lower point

tran $x = -4$

derivative
if $x = 0$
find y

13. The slope of the tangent line to the graph of $-3x^2 + cx - 3e^y = -3$ at $x = 0$ is 4. Give the value of c .

a. -6

b. 6

c. -3

d. -12

e. 12

14. Compute $\int 2^x - 4e^{2\ln x} dx$

a. $2^x \ln 2 - \frac{2e^{2\ln x}}{x} + c$

b. $2^x \ln 2 - 2e^{2\ln x} + c$

c. $\frac{2^x}{\ln 2} - \frac{4}{3}x^3 + c$

d. $\frac{2^x}{\ln 2} - 2e^{2\ln x} + c$

e. $\frac{2^x}{\ln 2} - 2x^2 + c$

15. What is the average value of the function $g(x) = (2x + 4)^2$ on the interval from $x = -4$ to $x = -1$?

a. -4

b. 4

c. 10

d. 12

e. 6

derivative
of $\tan x$

16. Compute $\lim_{t \rightarrow 0} \frac{\tan(\frac{1}{4}\pi + t) - \tan\frac{1}{4}\pi}{t}$

a. -1

b. 2

c. $\frac{1}{4}\pi$

d. π

e. 1

derivative of $\tan x$ at $x = \pi/4$

$$\frac{d}{dx} \tan x = \sec^2 x = \frac{1}{\sin^2 x} = \frac{1}{\sin^2 \frac{\pi}{4}} = \frac{1}{(\frac{\sqrt{2}}{2})^2} = \left(\frac{2}{\sqrt{2}}\right)^2 = \frac{4}{2} = 2$$

derivative

17. Find the instantaneous rate of change of $f(t) = (3t^3 - 4t + 4)\sqrt{t^2 + 3t + 4}$ at $t = 0$.

- a. $-\frac{3}{2}$ b. -8 c. -6 d. -5 e. -1

derivative

18. Compute $\frac{d}{dx} 7^{\cos x}$

- a. $-\sin x 7^{\cos x} \ln 7$ b. $\sin x 7^{\cos x} \ln 7$ c. $-\sin x 7^{\cos x}$ d. $-\frac{\sin x 7^{\cos x}}{\ln 7}$ e. $\frac{\sin x 7^{\cos x}}{\ln 7}$

19. A solid is generated by rotating the region enclosed by the graph of $y = \sqrt{x}$, the lines $x = 1$, $x = 2$, and $y = 1$, about the x -axis. Which of the following integrals gives the volume of the solid?

- a. $\int_1^2 \pi(x-1)^2 dx$ b. $\int_1^2 \pi(x-1) dx$ c. $\int_1^2 \pi(\sqrt{x}-1)^2 dx$ d. $\int_1^2 \pi(2-x)^2 dx$
e. $\int_1^2 \pi(2-\sqrt{x})^2 dx$

20. Compute $\lim_{x \rightarrow 0} \frac{2x}{\sin 3x} + \frac{x}{\cos 3x}$

- a. $\frac{2}{3}$ b. undefined c. 0 d. $\frac{1}{3}$ e. ∞

21. Given $y > 0$ and $\frac{dy}{dx} = \frac{3x^2 + 4x}{y}$. If the point $(1, \sqrt{10})$ is on the graph relating x and y , then what is y when $x = 0$?

- a. 6 b. 3 c. 1 d. 10 e. 2

22. Determine $\int_1^2 \frac{1}{\sqrt{4-t^2}} dt$

- a. π b. $\frac{1}{2}\pi$ c. $\frac{1}{3}\pi$ d. $\frac{1}{6}\pi$ e. $\frac{1}{4}\pi$

23. Determine $\int e^{2x} \sqrt{e^x + 1} dx$

- a. $\frac{2}{5}(e^x + 1)^{5/2} - 3(e^x + 1)^{3/2} + c$ b. $e^{2x}(e^x + 1)^{3/2} + c$ c. $\frac{2}{5}e^{5/2x} - 5e^{3/2x} + c$
d. $\frac{2}{5}(e^x + 1)^{5/2} + 3(e^x + 1)^{3/2} + c$ e. $\frac{2}{5}(e^x + 1)^{5/2} - \frac{2}{3}(e^x + 1)^{3/2} + c$

24. A particle's acceleration for $t \geq 0$ is given by $a(t) = 12t + 4$. The particle's initial position is 2 and its velocity at $t = 1$ is 5. What is the position of the particle at $t = 2$?

- a. 20 b. 10 c. 4 d. 16 e. 12

25. Determine $\int_0^{\frac{1}{2}\pi} \sin 3x \, dx + \int_0^{\frac{1}{6}\pi} \cos 3x \, dx$

- a. 0 b. $-\frac{2}{3}$ c. 1 d. -1 e. $\frac{2}{3}$

26. Determine the derivative of $f(x) = \cos^3(3x + 2)$ at $x = \frac{\pi}{3}$.

- a. $-9\cos^2(\pi + 2)\sin(\pi + 2)$ b. $-9\cos^2(\pi + 2)$ c. $-9\cos^2(\pi + 2)\sin(\pi + 2)$
 d. $27\cos^2(\pi + 2)\sin(\pi + 2)$ e. $27\cos^2(\pi + 2)$

27. Compute the derivative of $f(x) = \int_0^{x^2} \ln(t^2 + 1) \, dt$

- a. $\ln(x^2 + 1)$ b. $\frac{2x}{x^4 + 1}$ c. $2x \ln(x^2 + 1)$ d. $2x \ln(x^4 + 1)$ e. $\ln(x^4 + 1)$

28. Determine $\frac{d}{dx} \ln(\ln(2 - \cos x))$

- a. $\frac{\sin x(2 - \cos x)}{\ln(2 - \cos x)}$ b. $\frac{\sin x}{\ln(2 - \cos x)}$ c. $\frac{\cos x}{(2 - \cos x)\ln(2 - \cos x)}$ d. $-\frac{\cos x}{\ln(2 - \cos x)}$ e. $\frac{\sin x}{(2 - \cos x)\ln(2 - \cos x)}$

*derivative
 $\frac{d}{dx} \ln \frac{dy}{dx}$*



AB practice Test - packet

#1) $f(g(-2))$

$$\begin{aligned} &\downarrow \\ \frac{-2}{(-2)^2+1} &= f\left(\frac{-2}{5}\right) = \frac{-2}{5} - \frac{2.5}{1.5} = \frac{-2}{5} - \frac{10}{5} = \boxed{\frac{-12}{5}} \quad E \end{aligned}$$

#2) $f(x) = x^2 - 6\sqrt{x}$

$$f'(x) = 2x - 6 \cdot \frac{1}{2} x^{-1/2}$$

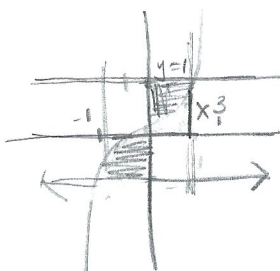
$$= 2x - \frac{3}{\sqrt{x}} \quad \text{at } x=4$$

$$f'(4) = 2(4) - \frac{3}{\sqrt{4}} = \frac{8-3}{1.2} = \frac{5}{1.2} = \frac{16}{2} - \frac{3}{2} = \boxed{\frac{13}{2}} \quad D$$

#3) $x \rightarrow \infty$ bottom is bigger than $\boxed{0}$ D

#4) $f(x) = x^3$

$$\boxed{2 \int_0^1 (1-x^3)} \quad E$$



$$\#5) \quad 5x^3 - 3xy - 2y^2 = 1$$

f'g + g'f'

$$15x^2 - 3\left[x \cdot 1 \frac{dy}{dx} + y \cdot 1\right] - 4y \frac{dy}{dx} = 0$$

$$15x^2 - 3x \frac{dy}{dx} - 3y - 4y \frac{dy}{dx} = 0$$

$$-3x \frac{dy}{dx} - 4y \frac{dy}{dx} = -15x^2 + 3y$$

$$\left(\cancel{-3x - 4y}\right) \frac{dy}{dx} = \frac{-15x^2 + 3y}{-3x - 4y}$$

$$\frac{dy}{dx} = \frac{-(15x^2 - 3y)}{-3x - 4y}$$

$$\boxed{\frac{dy}{dx} = -\frac{15x^2 - 3y}{-3x - 4y}} \quad C$$

$$\#6) \quad -3\sec x + 5\csc x$$

$$-3\sec x \tan x + 5(-\csc x \cot x)$$

$$\boxed{-3\sec x \tan x - 5\csc x \cot x} \quad D$$

#7) $\int_0^{1/4} \frac{16}{1+16t^2}$

$16 \int_0^{1/4} \frac{1}{1+(4t)^2} dt$

$u = 4t$
 $\frac{du}{4} = \frac{4dt}{4}$

$\frac{16}{4} \int_0^{1/4} \frac{1}{1+u^2} du$

$\frac{du}{4} = dt$

$\tan^{-1} = \frac{d}{1+u^2}$

$4 \int_0^{1/4} \frac{1}{1+u^2} du$

$4 \tan^{-1} u \Big|_0^{1/4}$

$4 \tan^{-1}(4t) \Big|_0^{1/4}$

$4 \tan^{-1}(4 \cdot \frac{1}{4}) - 4 \tan^{-1}(4 \cdot 0)$

$4 \tan^{-1}(1) - 4 \tan^{-1}(0)$

$4 \cdot \frac{\pi}{4} - 4 \cdot 0$

$\boxed{\pi} \text{ E}$

$$\#9) \frac{d}{dx} \frac{2x^4 - 4x}{2x^4 + 4x}$$

$$\frac{\cancel{2x}(x^3 - 2)}{\cancel{2x}(x^3 + 2)}$$

$$\frac{f'g - g'f}{g^2}$$

$$\frac{d}{dx} \frac{x^3 - 2}{x^3 + 2}$$

$$\frac{(3x^2)(x^3 + 2) - (3x^2)(x^3 - 2)}{(x^3 + 2)}$$

$$\frac{\cancel{3x^5} + 6x^2 - \cancel{3x^5} + 6x^2}{(x^3 + 2)}$$

$$\boxed{\frac{12x^2}{(x^3 + 2)}} \quad B$$

$$\#1) y = 4x\sqrt{x^2+4} - 2 \quad \text{at } (0, -2)$$

normal line = perpendicular slope

$$y' = 4x \cdot \frac{1}{2}(x^2+4)^{-1/2} \cdot 2x + \sqrt{x^2+4} \cdot 4$$

$$= \frac{4x^2}{\sqrt{x^2+4}} + \frac{4\sqrt{x^2+4}}{1}$$

$$= \frac{4(0)^2}{\sqrt{(0)^2+4}} + 4(\sqrt{(0)^2+4})$$

$$= 4\sqrt{4} = 4 \cdot 2 = \boxed{8} \quad \boxed{m=0}$$

$$y = mx + b$$

$$-2 = \frac{-1}{0}(0) + b$$

$$\boxed{-2 = b}$$

$$0(y = -\frac{1}{0}x - 2)$$

$$0y = -x - 10$$

$$\boxed{x + 0y = -10} \quad C$$

$fg' + gt'$

perpendicular slope

$$m = -\frac{1}{0}$$

$$\#10) \quad f(x) = 4 \sin x + 4 \cos^2 x \quad \text{at } x = \pi$$

$f''(x)$ tells us concavity —

$$f'(x) = 4 \cos x + 8 \cos x \cdot -\sin x$$

$$f'(x) = 4 \cos x - 8 \cos x \sin x$$

$fg' + gf'$

$$f''(x) = -4 \sin x - 8 [\cos x \cdot \cos x + \sin x \cdot -\sin x]$$

$$= -4 \sin x - 8 [\cos^2 x - \sin^2 x]$$

$$= -4 \sin x - 8 \cos^2 x + 8 \sin^2 x \quad \text{at } x = \pi$$

$$= -4 \sin(\pi) - 8 \cos^2(\pi) + 8 \sin^2(\pi)$$

$$= \cancel{-4(0)} - 8(-1)^2 + \cancel{8(0)^2}$$



$$= -8(1) = \boxed{-8} \text{ A}$$

concave
down

$$\#11) \int 4x^2 \sqrt{x^3+3} dx$$

$$4 \int x^2 \sqrt{x^3+3} dx$$

$$u = x^3 + 3$$

$$\frac{du}{3} = \frac{3x^2 dx}{3}$$

$$\frac{du}{3} = x^2 dx$$

$$\frac{4}{3} \int \sqrt{u} du$$

$$\frac{4}{3} \frac{u^{3/2}}{\frac{3}{2}} + C$$

$$\frac{4}{3} \cdot \frac{2}{3} u^{3/2} + C$$

$$\frac{8}{9} (x^3+3)^{3/2} + C$$

B

#12) $f(x) = x^3 + \frac{15}{2}x^2 + 12x - 2$ local min

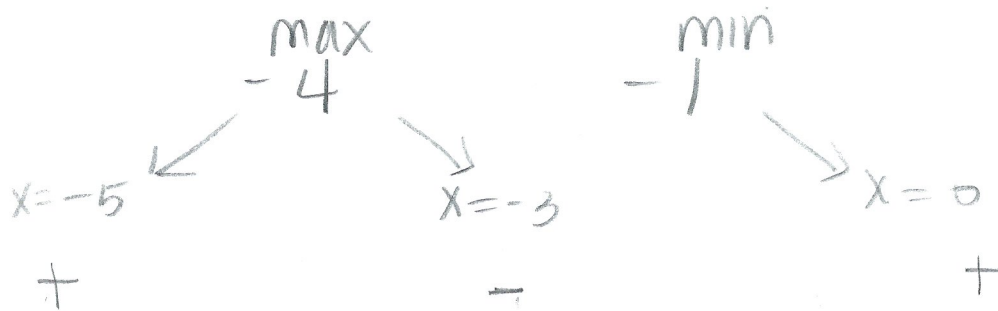
$$f'(x) = 3x^2 + 15x + 12$$

$$= 3x^2 + 15x + 12 = 0$$

$$= 3(x^2 + 5x + 4) = 0$$

$$= 3(x+4)(x+1) = 0$$

$$\boxed{x = -4} \quad \boxed{x = -1}$$



minimum at $x = -1$ B

$$\#13) -3x^2 + cx - 3e^y = -3 \text{ at } x=0 \text{ slope} = 4$$

$$-6x + c - 3e^y \cdot \downarrow \frac{dy}{dx} = 0$$

Find y

$$\frac{-3e^y}{-3e^y} \frac{dy}{dx} = \frac{6x - c}{-3e^y}$$

$$-3(0)^2 + c(0) - 3e^y = -3$$

$$\frac{-3e^y}{-3} = \frac{-3}{-3}$$

$$\ln e^y = \ln 1$$

$$y = 0$$

$$(0, 0)$$

$$\frac{dy}{dx} = \frac{6x - c}{-3e^y}$$

$$\frac{dy}{dx} = \frac{6(0) - c}{-3e^{(0)}} = 4$$

$$\frac{-c}{-3} = 4$$

$$-c = -12$$

$$\boxed{c = 12} \quad E$$

$$\#14) \int 2^x - 4e^{2\ln x} dx$$

$$\int 2^x - 4 \int (e^{\ln x})^2 dx$$

$$\int 2^x - 4 \int x^2 dx$$

$$\frac{2^x}{\ln 2} - \frac{4x^3}{3} + C$$

$$\boxed{\frac{2^x}{\ln 2} - \frac{4x^3}{3} + C} \quad C$$

#15)

$$\frac{1}{b-a} \int_a^b f(x) dx$$

$$\frac{1}{-1+4}$$

$$\frac{1}{3} \int_{-4}^{-1} (2x+4)^2 dx \quad u = 2x+4$$

$$\frac{du}{2} = \frac{2dx}{2}$$

$$\frac{1}{6} \int_{-4}^{-1} u^2 du \quad \frac{du}{2} = dx$$

$$\frac{1}{6} \frac{u^3}{3} \Big|_{-4}^{-1}$$

$$\frac{u^3}{18} \Big|_{-4}^{-1} = \frac{(2x+4)^3}{18} \Big|_{-4}^{-1}$$

$$\frac{(2(-1)+4)^3}{18} - \frac{(2(-4)+4)^3}{18}$$

$$\frac{8}{18} + \frac{+64}{18} = \frac{72}{18} = \boxed{4} B$$

$$\#16) \lim_{t \rightarrow 0} \frac{\tan(\frac{1}{4}\pi + t) - \tan \frac{1}{4}\pi}{t}$$

$$\frac{\tan \frac{\pi}{4} - \tan \frac{\pi}{4}}{0} = \frac{\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}}{0} = \frac{0}{0}$$

use L'Hopital's rule

$$f' = \frac{\sec^2(\frac{1}{4}\pi + t) \cdot 1 - \sec^2(\frac{1}{4}\pi) \cdot 0}{1}$$

$$\lim_{t \rightarrow 0}$$

$$\sec^2(\frac{1}{4}\pi + 0) - \sec^2(\frac{1}{4}\pi) \cdot 0$$

$$\sec^2(\frac{1}{4}\pi)$$

$$\sec^2(\frac{\pi}{4}) = \frac{1}{x}$$

$$\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right) = \frac{1}{\frac{\sqrt{2}}{2}} = \frac{2}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{2\sqrt{2}}{\sqrt{2}} = \sqrt{2}^2$$

$$= \boxed{2}$$

B

$$\#17) f(t) = (3t^3 - 4t + 4) \sqrt{t^2 + 3t + 4} \quad \text{at } t=0$$

Slope $fg' + gf'$

$$f'(t) = (3t^3 - 4t + 4) \cdot \frac{1}{2}(t^2 + 3t + 4)^{-1/2} (2t + 3)$$

$$+ \sqrt{t^2 + 3t + 4} \cdot (9t^2 - 4)$$

at $x=0$

$$f'(0) = 4 \cdot \frac{1}{2} \cdot 4^{-1/2} \cdot 3 + \sqrt{4} \cdot (-4)$$

$$= \frac{2}{\sqrt{4}} \cdot 3 + 2 \cdot (-4)$$

$$= \frac{2}{1} \cdot 3$$

$$= 3 + -8 = \boxed{-5} \text{ D}$$

$$\#18) \frac{d}{dx} 7^{\cos x}$$

$$7^{\cos x} \cdot \ln 7 \cdot -\sin x$$

$$\boxed{-\sin x \cdot 7^{\cos x} \cdot \ln 7} \quad A$$

#19)



$$\textcircled{O} \quad \pi(R^2 - r^2)$$

$$\int_1^2 \pi((\sqrt{x})^2 - 1^2)$$

$$\boxed{\int_1^2 \pi(x-1) dx} \quad B$$

$$\#20) \lim_{x \rightarrow 0} \frac{2x}{\sin 3x} + \frac{x}{\cos 3x}$$

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

$$\lim_{x \rightarrow 0} \frac{2x}{\sin 3x} + \lim_{x \rightarrow 0} \frac{x}{\cos 3x}$$

$$\frac{2(0)}{\sin(0)} \quad \frac{0}{\cos(0)}$$

$$\frac{0}{0} \quad \frac{0}{1}$$

Use L'Hopital's
rule

+ 0

$$f' = \frac{2}{\cos 3x \cdot 3}$$

$$\lim_{x \rightarrow 0} = \frac{2}{3 \cos 3x}$$

$$\frac{2}{3 \cos(0)}$$

$$\frac{2}{3 \cdot 1}$$

$$\frac{2}{3} + 0 = \boxed{\frac{2}{3}}$$

$$\#21) \frac{dy}{dx} = \frac{3x^2 + 4x}{y}$$

$$\int y dy = \int (3x^2 + 4x) dx$$

$$\frac{y^2}{2} = \frac{3x^3}{3} + \frac{4x^2}{2} + C$$

$$\frac{y^2}{2} = x^3 + 2x^2 + C$$

$$y^2 = 2x^3 + 4x^2 + 2C \quad \text{point } (1, \sqrt{10})$$

$$(\sqrt{10})^2 = 2(1)^3 + 4(1)^2 + 2C$$

$$10 = 2 + 4 + 2C$$

$$10 = 6 + 2C$$

$$-6 \quad -6$$

$$4 = 2C$$

$$C = 2$$

$$y^2 = 2x^3 + 4x^2 + 4 \quad \text{when } x=0$$

$$\sqrt{y^2} = \sqrt{4}$$

$$y = \pm 2 \quad \text{and } y > 0$$

$$\boxed{y = 2} \in$$

$$\#22) \int_1^2 \frac{1}{\sqrt{4-t^2}} dt$$

we need $4-t^2 = 1-(\quad)^2$

$$2^2 - t^2$$

$$\sqrt{4(1-\frac{1}{4}t^2)}$$

$$2\sqrt{1-(\frac{1}{2}t)^2}$$

$$2 \int_1^2 \frac{1}{\sqrt{1-(\frac{1}{2}t)^2}} dt$$

$$\frac{2}{2} \int_1^2 \frac{1}{\sqrt{1-u^2}} du$$

$$|\sin^{-1} u|_1^2$$

$$|\sin^{-1}(\frac{1}{2}t)|_1^2$$

$$\sin^{-1}(\frac{1}{2} \cdot 2) - \sin^{-1}(\frac{1}{2})$$

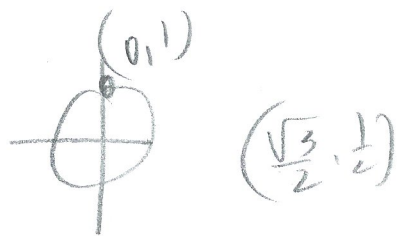
$$\sin^{-1}(1) - \sin^{-1}(\frac{1}{2})$$

$$4 \cdot \frac{\pi}{2} - \frac{\pi}{6}$$

$$u = \frac{1}{2}t$$

$$du = \frac{1}{2} dt$$

$$2 du = dt$$



$$\frac{1}{\sqrt{a^2-x^2}} = \sin^{-1} \frac{x}{a}$$

$$= \sin^{-1} \frac{t}{2}$$

$$\frac{\pi}{6} - \frac{\pi}{6}$$

$$\frac{3}{6} - \frac{\pi}{6} = \frac{2\pi}{6} = \frac{\pi}{3} C$$

$$\#23) \int e^{2x} \sqrt{e^x + 1} dx$$

$$\int e^x \cdot e^x \sqrt{e^x + 1} dx$$

$$\int e^x \sqrt{e^x + 1} \cdot e^x dx$$
$$\int (u-1) \sqrt{u} du$$

$$\int (u-1) u^{1/2} du$$

$$\int u^{3/2} - u^{1/2} du$$

$$\frac{u^{5/2}}{5/2} - \frac{u^{3/2}}{3/2} + C$$

$$\frac{2}{5} u^{5/2} - \frac{2}{3} u^{3/2} + C$$

$$\boxed{\frac{2}{5} (e^x + 1)^{5/2} - \frac{2}{3} (e^x + 1)^{3/2} + C}$$

E

$$u = e^x + 1$$
$$du = e^x dx$$

since

$$u = e^x + 1$$

$$u - 1 = e^x$$

as well

$$\#24) a(t) = \int 12t + 4$$

$$v(t) = \frac{12t^2}{2} + 4t + C$$

$$v(t) = 6t^2 + 4t + C \quad t=1 \text{ is } 5 = v(t)$$

$$5 = 6(1)^2 + 4(1) + C$$

$$5 = 6 + 4 + C$$

$$5 = 10 + C$$

$$\boxed{5 = C}$$

$$v(t) = \int 6t^2 + 4t - 5$$

position

$$s(t) = \frac{6t^3}{3} + \frac{4t^2}{2} - 5t + C$$

$$s(t) = 2t^3 + 2t^2 - 5t + C$$

initial position

$$s(t) = 2t^3 + 2t^2 - 5t + 2$$

at $t=2$
position = ?

$$s(2) = 2(2)^3 + 2(2^2) - 5(2) + 2$$

$$= 16 + 8 - 10 + 2$$

$$= 24 - 10 + 2$$

$$= 14 + 2 = \boxed{16} \quad D$$

#25) Determine

$$\int_0^{\frac{1}{2}\pi} \sin 3x \, dx + \int_0^{\frac{1}{6}\pi} \cos 3x \, dx$$

$$\begin{aligned} u &= 3x \\ \frac{du}{3} &= \frac{3}{3} dx \\ \frac{du}{3} &= dx \end{aligned}$$

$$\begin{aligned} u &= 3x \\ du &= 3dx \\ \frac{du}{3} &= dx \end{aligned}$$

$$\frac{1}{3} \int_0^{\frac{\pi}{2}} \sin u \, du$$

$$\frac{1}{3} \int_0^{\frac{\pi}{6}} \cos u \, du$$

$$-\frac{1}{3} \cos 3x \Big|_0^{\frac{\pi}{2}}$$

$$\frac{1}{3} \sin 3x \Big|_0^{\frac{\pi}{6}}$$

$$-\frac{1}{3} \cos \frac{3\pi}{2} + \frac{1}{3} \cos(0) + \frac{1}{3} \sin \frac{\pi}{6} - \frac{1}{3} \sin(0)$$

$$+\frac{1}{3}(1) + \frac{1}{3}(1) -$$

$$+\frac{1}{3} + \frac{1}{3}$$

$$\boxed{\frac{2}{3}} \text{ E}$$

$$\#29) \frac{d}{dx} \ln(\ln(2-\cos x))$$

$$\frac{1}{\ln(2-\cos x)} \cdot \frac{1}{(2-\cos x)} \cdot +\sin x$$

$$\frac{\sin x}{\ln(2-\cos x)(2-\cos x)}$$

E

$$\#26) f(x) = \cos^3(3x+2) \quad \text{at } x = \frac{\pi}{3}$$

$$f'(x) = 3 \cos^2(3x+2) \cdot -\sin(3x+2) \cdot 3$$
$$= -9 \cos^2(3x+2) \sin(3x+2)$$

$$\boxed{-9 \cos^2(\pi+2) \sin(\pi+2)} \quad A$$

$$\#27) \frac{d}{dx} f(x) = \frac{d}{dx} \int_0^{x^2} \ln(t^2+1) dt$$

derivative of x^2

$$f'(x) = \ln((x^2)^2+1) \cdot 2x$$

$$= \ln(x^4+1) \cdot 2x$$

$$= \boxed{2x \ln(x^4+1)} \quad D$$

Exchange
exponent
to a
3